

Algebra 2 Notes

Name: key

Section 2.4 – Writing Linear Functions

DAY ONE:

Recall from Section 2.3 that the slope-intercept form of a linear equation is $y = mx + b$, where m is the slope and b is its y -intercept.

In order to write an equation of a line in slope-intercept form, you would need both the slope and y -intercept.

Example 1: Write the equation of the graphed line in slope-intercept form.

a.

$m = -\frac{2}{5}$
 $b = 2$

$y = -\frac{2}{5}x + 2$

b.

$m = \frac{3}{4}$
 $b = -3$

$y = \frac{3}{4}x - 3$

Slope Formula		
Words	Algebra	Graph
Given two points on a line, the slope is the ratio of the difference in the y -values to the difference in the corresponding x -values, or rise over run.	The slope of the line containing (x_1, y_1) and (x_2, y_2) is $m = \frac{y_2 - y_1}{x_2 - x_1}$	

Example 2: Find the slope of each line.

a. line through $(3, -2)$ & $(-1, 2)$

$m = \frac{-2 - 2}{3 - (-1)}$
 $m = \frac{-4}{4}$
 $m = -1$

b.

x	2	5	8	11
y	1	6	11	16

$m = \frac{\Delta y}{\Delta x}$
 $m = \frac{5}{3}$

c.

$m = \frac{\text{rise}}{\text{run}}$
 $m = \frac{3}{0}$
 $m = \text{undefined}$

Because the slope of a line is constant, it is possible to use ANY point of a line and the slope of the line to write an equation of the line in point-slope form.

Point-Slope Form

The equation of a line with a slope of m and the point (x_1, y_1) is $y - y_1 = m(x - x_1)$.

Example 3: Write the equation of each line in slope intercept form.

a.

x	-3	-1	1	3
y	1.5	1	0.5	0

$$m = \frac{\Delta y}{\Delta x}$$

$$m = \frac{-0.5}{2}$$

$$m = -\frac{1}{4}$$

$$y - y_1 = m(x - x_1)$$

$$y - 0 = -\frac{1}{4}(x - 3)$$

$$y = -\frac{1}{4}x + \frac{3}{4}$$

use
point
(3,0)

b. with slope -5 and through the point $(1,3)$

$$y - y_1 = m(x - x_1)$$

$$y - 3 = -5(x - 1)$$

$$y - 3 = -5x + 5$$

$$y = -5x + 8$$

c. through the points $(-2, -3)$

and $(2,5)$

$$(-2, -3)$$

$$m = \frac{5 - (-3)}{2 - (-2)}$$

$$m = \frac{8}{4}$$

$$m = 2$$

$$y - y_1 = m(x - x_1)$$

$$y - (-3) = 2(x - (-2))$$

$$y + 3 = 2x + 4$$

$$y = 2x + 1$$

Example 4: Application

In the game of Monopoly, a player who lands on a property that is owned by another player must pay rent to the owner of the property. For most color properties, the rent can be modeled by a linear function of the selling price.

(a) Express the rent as a function of the selling price.

Monopoly Price and Rates		
Property Name	Selling Price (\$)	Rent (\$)
Mediterranean Avenue	60	2
Vermont Avenue	100	6
Tennessee Avenue	180	14
Marvin Gardens	280	24
Pennsylvania Avenue	320	28

$$m = \frac{\Delta \text{rent}}{\Delta \text{selling price}}$$

$$m = \frac{4}{40}$$

$$m = \frac{1}{10}$$

$$y - y_1 = m(x - x_1)$$

$$y - 2 = \frac{1}{10}(x - 60)$$

$$y - 2 = \frac{1}{10}x - 6$$

$$y = \frac{1}{10}x - 4$$

(b) How much is the rent for Illinois Avenue, which has a selling price of \$240?

$$x = 240$$

$$y = \frac{1}{10}(240) - 4$$

$$y = 24 - 4$$

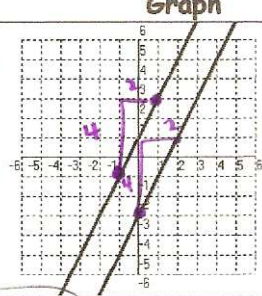
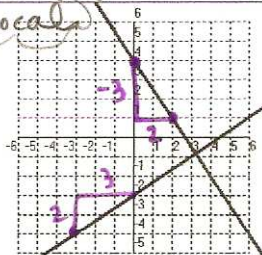
$$y = 20$$

$$\boxed{\$20}$$

DAY TWO:

By comparing slopes, you can determine if lines are parallel or perpendicular. You can also write equations of lines that meet certain needs.

\parallel = parallel \perp = perpendicular

Parallel and Perpendicular Lines		
Words	Algebra	Graph
Parallel Lines - If both slopes are defined, the slopes of parallel lines are equal. The slopes of parallel vertical lines are undefined.	$y_1 = 2x + 1 \quad m_1 = 2$ $y_2 = 2x + 3 \quad m_2 = 2$ $2 = 2$ <i>same</i> $m_1 = m_2$ <i>parallel</i>	 $m_1 = \frac{4}{2}$ $m_1 = 2$ $m_2 = \frac{4}{2}$ $m_2 = 2$
Perpendicular Lines - If both slopes are defined, the slopes of perpendicular lines are opposite reciprocals. Their product is -1 . A vertical line and a horizontal line are perpendicular.	$y_1 = -\frac{3}{2}x + 4 \quad m_1 = -\frac{3}{2}$ $y_2 = \frac{2}{3}x - 3 \quad m_2 = \frac{2}{3}$ $(-\frac{3}{2})(\frac{2}{3}) = -1 \checkmark$ \perp	 $m_1 = -\frac{3}{2}$ $m_2 = \frac{2}{3}$

Example 1: Given the slope of a line, find the slope of a line that is parallel to it and the slope of a line that is perpendicular to it.

a. $\frac{2}{3}$ $m_{\parallel} = \frac{2}{3}, m_{\perp} = -\frac{3}{2}$	b. -5 $m_{\parallel} = -5$ $m_{\perp} = \frac{1}{5}$	c. 1 $m_{\parallel} = 1$ $m_{\perp} = -1$	d. 0 $m_{\parallel} = 0$ $m_{\perp} = \text{undefined}$	e. $-\frac{5}{2}$ $m_{\parallel} = -\frac{5}{2}$ $m_{\perp} = \frac{2}{5}$
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Example 2: Determine if each pair of lines is parallel, perpendicular, or neither.

a. $x + y = 5 \rightarrow y = -x + 5$ $x - y = -6 \rightarrow y = x + 6$ $m = -1$ $m = 1$ \perp	b. $2x + 3y = 6 \rightarrow y = -\frac{2}{3}x + 2$ $3y = -2x + 6 \rightarrow y = -\frac{2}{3}x + 2$ $m = -\frac{2}{3}$ $m = -\frac{2}{3}$ \parallel	c. $x = 5$ $y = -2$ $m = \text{undefined}$ $m = 0$ \perp
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Example 3: Write the equation of each line in slope-intercept form.

a. parallel to $y = 1.5x + 6$ & through $(4, 5)$ \uparrow $m = 1.5$ or $\frac{3}{2}$ $\text{so } m_{\parallel} = \frac{3}{2}$ $y - y_1 = m(x - x_1)$ $y - 5 = \frac{3}{2}(x - 4)$ $y - 5 = \frac{3}{2}x - 6$ $y = \frac{3}{2}x - 1$	b. perpendicular to $y = -\frac{3}{4}x + 2$ & through $(6, -4)$ \uparrow $m = -\frac{3}{4}$ $\text{so } m_{\perp} = \frac{4}{3}$ $y - y_1 = m(x - x_1)$ $y + 4 = \frac{4}{3}(x - 6)$ $y + 4 = \frac{4}{3}x - 8$ $y = \frac{4}{3}x - 12$
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